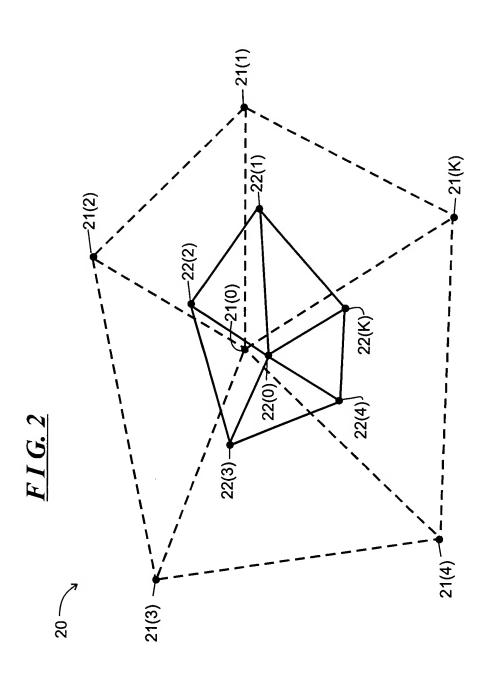
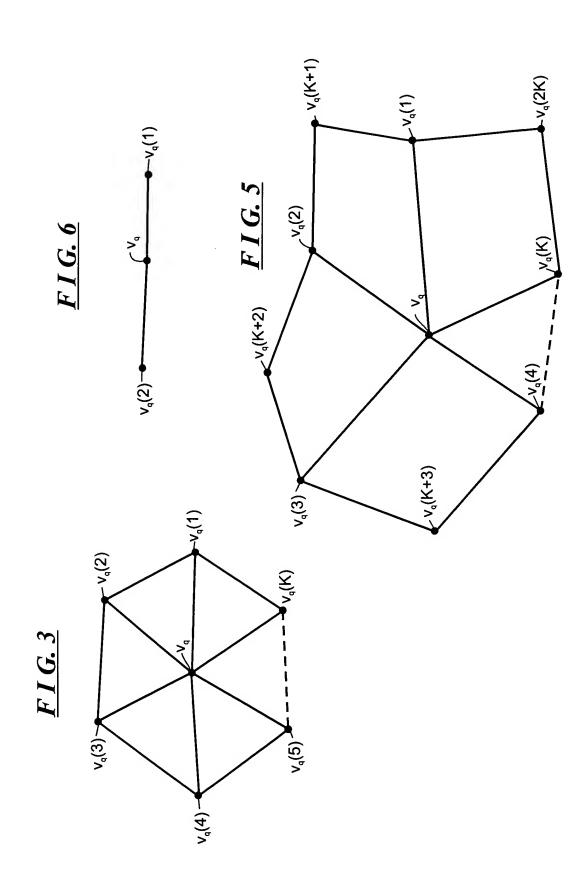
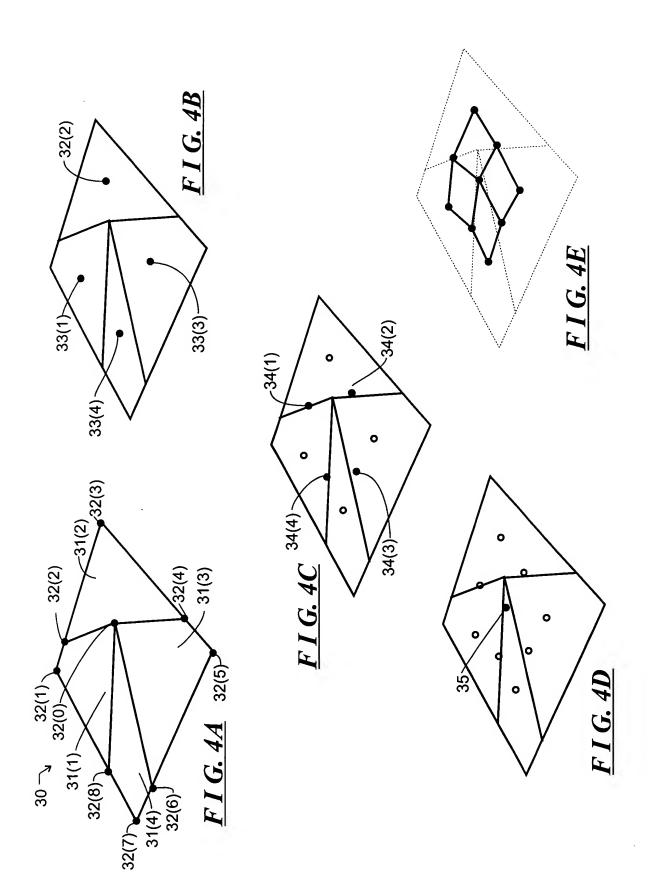


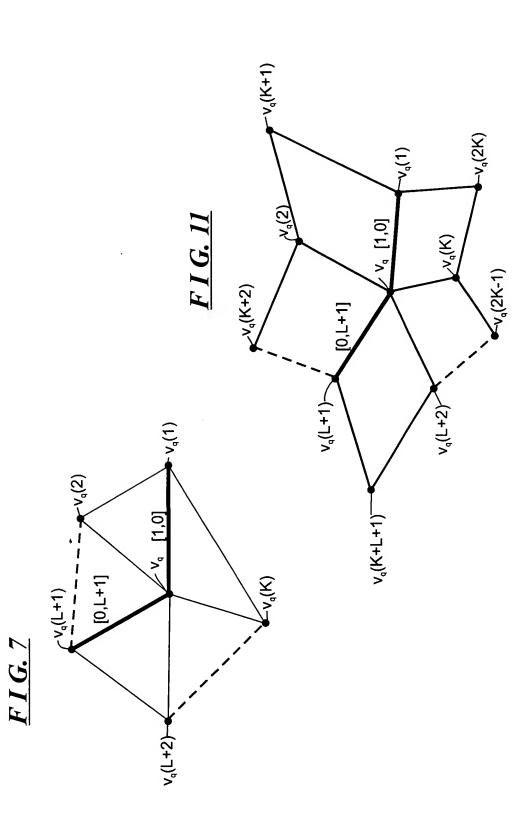
FIG.1







ASTRONAL



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                                                                    -0.0098265,
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                                         -0.0072665,
                                                       -0.00732092,
                                                                    -0.00984525},
(0.0241408,
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                           -0.00729284,
                                        -0.00984683}}}
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{{{-0.301785} {0.705044, -0.0432493, {0.276585,	, 0.174949, -0.125369, -0.0578848, -0.106806,	-0.133614, 0.125961, 0.00208289, 0.0710183,	-0.209551}, -0.00701645, 0.11396, 0.162541}},	0.0422859, -0.0510825},	
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{{-0.138635, {0.388516, -0.189469, {0.401914, 0.234623, {0.292433, 0.119528, {0.00306035,	0.149761, 0.0502042, -0.00768783, -0.0679866, -0.0727325, -0.0313445, -0.0377854, -0.0101548,	-0.144616, 0.17695, 0.0782015, -0.178113, -0.10786, -0.0445371, -0.0494528, 0.00637489,	-0.0583901}, -0.0367233, 0.14955, 0.134779, -0.160807, 0.0666588, -0.0736189, 0.00427581}}	-0.145073, 0.142332}, 0.201924, -0.179405}, 0.100615, -0.0872955},	



100. INITIALIZE THE SUBDIVISION MATRICES S\_{sc,T,K,L}(S\_{1}(J),S\_{2}(J)), J=0,1,2 AS DESCRIBED IN CONNECTION WITH EQUATION (19)

(101. GENERATE THE MATRIX PRODUCTS S\_{sc,T,K,L,LP}(J)(S\_{1},S\_{2}) FOR J=2,3; FOR J=1, S\_{sc,T,K,L,LP}(1)(S\_{1},S\_{2})=S\_{sc,T,K,L}(S\_{1},S\_{2}), AND FOR J=0, S\_SC,T,K,L,LP}(0)(S\_{1},S\_{2}) IS THE ("K+1"-BY-"K+1" IDENTITY MATRIX I\_{K+1}

(102. USE THE FIRST ROW OF EACH MATRIX PRODUCT S\_{sc,T,K,L,LP}(J)(S\_{1},S\_{2}), J=0, 1, 2, 3, TO GENERATE COMPONENT-WISE AN APPROXIMATION TO LIMIT POINT WEIGHT VECTOR I\_{LP} IN ACCORDANCE WITH THE EXTRAPOLATION FORMULA IN EQUATION (41)

(103. USE THE MATRIX PRODUCTS

S\_{sc,T,K,L,LP}(J)(S\_{1},S\_{2}), DILATION FACTOR d(K)

AND VECTORS v\_{C} AND v\_{S} TO GENERATE THE

VECTORS I\_{C}(J) AND I\_{S}(J), J=1, 2, AND 3 AS

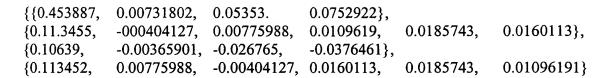
DESCRIBED IN CONNECTION WITH EQUATION (43); FOR

J=0, THE RESPECTIVE TANGENT VECTOR WEIGHT

VECTORS ARE I\_{C}(0)=v\_{C} AND I\_{S}(0)=v\_{S}

104. USE VECTORS I\_{C}(J) AND I\_{S}(J) TO GENERATE APPROXIMATIONS TO THE TANGENT VECTOR WEIGHT VECTORS I\_{C} AND I\_{S} IN ACCORDANCE WITH EQUATION (46)

105. USE THE LIMIT POINT WEIGHT VECTOR I\_{LP} AND TANGENT VECTOR WEIGHT VECTORS I\_{C} AND I\_{S}, ALONG WITH THE POSITIONS OF THE VERTEX v\_{q}(0) AND NEIGHBORING POINTS v\_{q}(1) THROUGH v\_{q}(K) TO GENERATE THE LIMIT POINT AND TANGENT VECTORS AS DESCRIBED IN CONNECTION WITH EQUATIONS (30) AND (37), RESPECTIVELY; THE NORMAL VECTOR CAN ALSO BE GENERATED AS THE CROSS PRODUCT BETWEEN THE TANGENT VECTORS



{{-2.05162,	3.04791,	-2.76216,	-0.993681},	
{395871,	0.244816,	1.63404,	-0.196152,	-0.99494,
-1.46708,	-0.0446372,	0.421901,	1.08452,	1.28361},
{1.02581,	-1.52396,	1.38108,	0.49684},	
{-3.95871,	-1.63404,	-0.244816,	1.46708,	0.99494,
0.196152.	-1.28361.	-1.08452.	-0.421901.	0.0446372}}

### F I G. 13